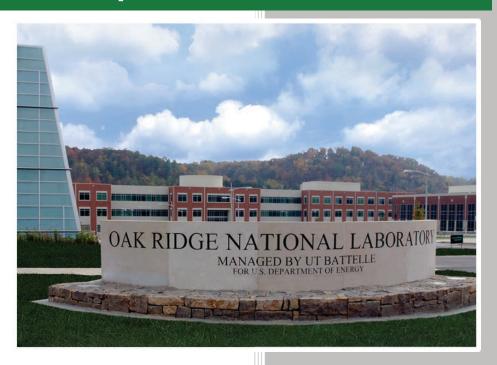
Measurement of Average Burnup in TRISO-Coated Particles from AGR-2 UCO Compacts 2-2-2 and 6-4-2



Fred C. Montgomery John D. Hunn Tamara J. Keever Benjamin D. Roach Ralph H. Ilgner Emilie K. Fenske Joseph M. Giaquinto

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Fusion and Materials for Nuclear Systems Division

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ACRONYMS

at% Atomic percent

AGR Advanced Gas Reactor (Fuel Development and Qualification Program)

AGR-2 Second AGR program irradiation experiment

ATR Advanced Test Reactor

BWXT-NOG BWX Technologies Nuclear Operations Group CCCTF Core Conduction Cooldown Test Facility CHAR-DAM Characterization data acquisition method

CO Carbon monoxide

FIMA Fission per initial metal atom HPIC High-pressure-ion-chromatography

ICP-MS Inductively-coupled plasma mass spectrometry

ID Identification

ID-HPIC-ICP-MS Isotope-dilution high-pressure-ion-chromatography ICP-MS

ID-ICP-MS Isotope-dilution ICP-MS

IFEL Irradiated Fuels Examination Laboratory (hot cells)

IMGA Irradiated Microsphere Gamma Analyzer IPyC Inner pyrolytic carbon (TRISO layer)

LBL Leach-burn-leach

LDPE Low-density polyethylene

NACIL Nuclear Analytical Chemistry & Isotopics Laboratory

OPyC Outer pyrolytic carbon (TRISO layer)
ORNL Oak Ridge National Laboratory
PIE Post-irradiation examination
PTFE Polytetrafluoroethylene
SiC Silicon carbide (TRISO layer)

 $\begin{array}{ll} TA_{min} & Time\mbox{-averaged minimum temperature} \\ TA_{max} & Time\mbox{-averaged maximum temperature} \end{array}$

TAVA Time-averaged/volume-averaged temperature

TGA/DTA Thermogravimetric analysis/differential thermal analyzer (analysis)

TRISO Tristructural-isotropic (coated particles)

UCO Uranium carbide/uranium oxide mixture (fuel kernels)

wt% weight-percent

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1. INTRODUCTION

Burnup analysis was performed on tristructural-isotropic (TRISO)-coated particles deconsolidated from compacts irradiated by the Advanced Gas Reactor (AGR) Fuel Development and Qualification Program in the second irradiation experiment (AGR-2) [Collin 2014]. The AGR-2 irradiation experiment included TRISO fuel particles with kernels containing both uranium oxide and uranium carbide, called UCO, where uranium carbide is included with the commonly-used uranium oxide in the kernel to provide a getter for oxygen liberated during fission and limit CO production. This allows the UCO-TRISO particles to be taken to higher burnup without failure from excessive internal CO pressure or CO-corrosion of the SiC layer. The UCO kernels were fabricated and coated at BWX Technologies Nuclear Operations Group (BWXT-NOG) with a 150-mm-diameter engineering-scale coater. The UCO-TRISO batch used in the AGR-2 irradiation experiment was Batch 93073, which had kernels with an average diameter of 426.7 µm and average coating thicknesses moving out from the kernel of 98.9 um (buffer), 40.4 um (IPvC). 35.2 µm (SiC), 43.4 µm (OPyC) [Barnes and Marshall 2009]. The TRISO particle were shipped to ORNL to be formed into compacts for irradiation testing. The compact lot qualified for the AGR-2 irradiation test was lot LEU09-OP2-Z and had an average of 3176 UCO-TRISO particles in each compact [Hunn, Montgomery, and Pappano 2010]. Compilations of the properties data for the particles and compacts are available in a pre-irradiation characterization summary report for the AGR-2 fuel composites [Hunn, Savage, and Silva 2010].

Compacts 2-2-2 and 6-4-2 were irradiated in the Advanced Test Reactor (ATR). Table 1 shows the calculations for expected burnup in percent fission per initial metal atom (FIMA), the fast neutron fluence (neutron energies E > 0.18 MeV), and calculated compact temperatures during irradiation. Safety testing was performed on both of these compacts in the ORNL Core Conduction Cooldown Test Facility (CCCTF), where they were heated to 1600 °C and held at that temperature for 300 h. Results from these safety tests are reported in [Hunn et al. 2016] and [Hunn et al. 2017]. After safety testing, compacts were subjected to the standard suite of destructive post-irradiation examination (PIE) described in detail in [Hunn et al. 2013]. Compact 2-2-2 was electrolytically deconsolidated and TRISO particles were separated from the matrix debris after preburn leaching for survey with the ORNL Irradiated Microsphere Gamma Analyzer (IMGA). After IMGA, an ~90% fraction of the TRISO particles was subjected to burnleach analysis (matrix debris was subjected to a separate burn-leach). Compact 6-4-2 was also electrolytically deconsolidated but TRISO particles, together with the matrix debris, were subjected to leach-burn-leach (LBL) and the full IMGA survey was not performed. Results from post-safety test PIE of Compact 6-4-2 are documented in [Hunn et al. 2018].

Table 1. Calculated irradiation conditions for AGR-2 UCO Compacts 2-2-2 and 6-4-2

Compact ID ^a	Fabrication ID ^b	Expected Burnup ^c (FIMA)	Fast Fluence c	Temperature ^d		
Compact 1D			(E>0.18 MeV)	TAVA	TA_{min}	TA_{max}
AGR-2 2-2-2	LEU09-OP2-Z075	12.55%	3.39E25 n/m ²	1287 °C	1189 °C	1354 °C
AGR-2 6-4-2	LEU09-OP2-Z049	9.26%	$2.21E25 \text{ n/m}^2$	1018 °C	894 °C	1106 °C

^a The X-Y-Z compact identification (ID) convention denotes the location in the irradiation test train: Capsule-Level-Stack [Collin 2014].

^b Physical properties data for individual compacts recorded in [Hunn, Montgomery, and Pappano 2010, 60–69].

^c Expected burnup [Sterbentz 2014, table 6] and fast fluence [Sterbentz 2014, table 12] are based on physics calculations.

^d Time-averaged, volume-averaged (TAVA) temperature, time-averaged minimum (TA_{min}) temperature, and time-averaged maximum (TA_{max}) temperature are based on thermal calculations [Hawkes 2014, table 3].

2. IFEL EXPERIMENTAL PROCEDURE

Random samples of post-LBL particles were counted, pulverized, burned, leached with hot nitric acid, leachates weighed, and aliquots prepared for transfer from the hot cell facilities in the Irradiated Fuels Examination Laboratory (IFEL) to the Nuclear Analytical Chemistry & Isotopics Labs (NACIL) using characterization data acquisition method AGR-CHAR-DAM-49 [Montgomery and Hunn 2018].

2.1 PREPARING PARTICLE SAMPLES

Sample preparation was done in the IMGA hot cell where contaminations levels are relatively low, compared to the main IFEL hot cells. Particle samples for burnup analysis were chute riffled from the particles collected from the LBL vessel after the burn-leach. The Compact 6-4-2 particle samples were riffled from a collection of all the particles in the compact, so random sampling error should be limited to the error introduced by chute riffling. While this error is dependent on the particle properties and their variability, experiments carried out by Khan in 1968 found that chute riffling of a binary mixture of fine and coarse sand introduce a 1% standard deviation in the measured size [Allen 1981]).

The Compact 2-2-2 particle samples were taken from a subset of the particles deconsolidated from the compact (~10% were set aside as a TRISO-coated archive), but this is not expected to have introduced significant additional sampling error. The ~90% fraction used for Compact 2-2-2 burn-leach was chute riffled from the full deconsolidated particle collection with the exception of 23 particles. Twenty of these particles were randomly dropped during gamma survey by the IMGA automated vacuum needle handling system and subsequently not added back into the sample to prevent chance of cross-contamination with particles from other compacts; exclusion of these 20 particles will not impact the sampling error. The other three particles were removed during the IMGA survey because of low ¹⁴⁴Ce and ¹³⁷Cs activity. These three particles had radioisotope inventories consistent with other occasionally-observed particles that evidently started the irradiation with abnormally-low ²³⁵U content and are presumed to have contained natural uranium UCO kernels that were somehow mixed in with the low-enriched uranium test fuel, based on analysis of similar particles found during AGR-1 PIE [Hunn et al. 2013, 36]. Removal of the three suspect particles before riffling out the burnup samples is actually beneficial for the burnup analysis, as particles that started the irradiation with abnormally-low ²³⁵U content would skew the results.

For each compact, two samples of ~200 particles each were riffled close to the target number of 200. The riffled samples were imaged and counted to determine the number of particles and a few particles were randomly removed or added from another small, riffled sample to bring the total close to 200. Images of Samples 222-A, 222-B, 642-A, and 642-B are shown in Figure 1 and Figure 2.

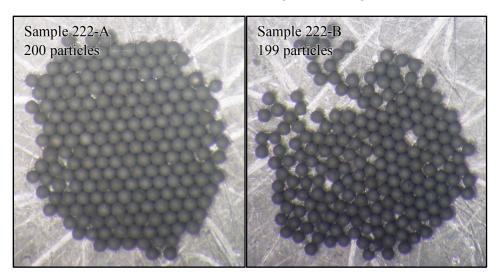


Figure 1. Images used to count particle samples from Compact 2-2-2 (arbitrary scaling).

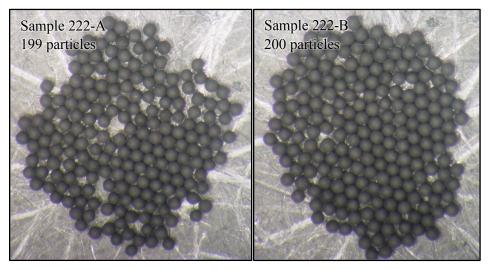


Figure 2. Images used to count particle samples from Compact 6-4-2 (arbitrary scaling).

2.2 PULVERIZING PARTICLES

While still in the IMGA cell, the two particle samples from each compact were placed in low-density polyethylene (LDPE) 15-ml narrow-mouth Nalgenetm bottles from ThermoFisher Scientific selected for containment of the samples during pulverization in the SPEXTM SamplePrep 8000M mill (Figure 3). The bottles had been previously prepared by labeling, weighing, preloading with about 5 g (55 spheres) of 3-mm yttria-stabilized zirconia grinding media from Tosoh, and reweighing. The bottles containing the samples were bagged to minimize pickup of contamination, then passed through and removed from the IFEL main hot cells. Working in a radiological hood in the IFEL charging area, each SPEXTM mill bottle was removed from the bag and weighed on a three-place Ohaus Pioneer analytical balance (±0.002g or ±0.002%, whichever is greater) to obtain the particle weight. The bottle was placed in the secondary SPEXTM mill container shown in Figure 3 and clamped in the SPEXTM mill. The sample was shaken for 20 minutes in a figure-8 motion that included short lateral movements combined with back-and-forth swings. After milling, the bottle was removed from the secondary SPEXTM mill container after a radiological smear verified that the bottle did not leak and contaminate the outer surface. The bottles were then bagged and transferred back to the main hot cell.



Figure 3. SPEXTM mill bottle (left), secondary SPEXTM mill container with O-ring seal (center), and secondary SPEXTM mill container lid (right).

2.3 BURNING SPEXTM MILL BOTTLE AND PULVERIZED PARTICLES

Each SPEXTM mill bottle containing a pulverized particle sample was placed in a new quartz Soxhlet thimble, shown on the left in Figure 4, which was fitted with a #2 fritted disk (40–90-μm porosity). The thimble was placed into a new quartz 250-ml flat-bottom flask which had a 45/50 ground glass neck, as shown in the center of Figure 4. The flask had a quartz manipulator grip attached to the neck to assist in remote operations. The assembly, without the polytetrafluoroethylene (PTFE) fitting shown in the figure, was covered with a raised, loose fitting cap and was placed into a Neytech Vulcan 3-550 box furnace. The cap protected the sample from contamination and allowed circulation of air into the flask. It had indentations in the lid that held it up off the rim of the flask and had sides which extended over and down the neck.



Figure 4. Soxhlet thimble with fritted glass disk in bottom (left), quartz reflux flask with manipulator grip and PTFE bushing (center), and ground-glass joint adapter for coupling to Soxhlet extractor (right).

This heating cycle was based on simultaneous thermogravimetric analysis/differential thermal analysis (TGA/DTA) with a TA Instruments Q600 TGA/DTA of the decomposition of LDPE cut from a NalgeneTM bottle. Figure 5 shows the weight-percent (wt%) loss and temperature difference between the sample and a reference thermocouple as the sample was heated in air at 10 °C/min. The LDPE began to lose weight around 250 °C with the rate of weight loss increasing until 390 °C where the specimen was losing weight at 16 wt%/min. Associated with this weight loss was a strong exothermic reaction. The rate of weight loss then slowed until about 400 °C when a second exothermic reaction occurred, resulting in a maximum rate at 423 °C of 8.1 wt%/min. Because of a concern about the possible loss of sample caused by air turbulence during these rapid exothermic reactions, the temperature ramp rate was reduced to 1 °C/min between 300 °C and 600 °C (Table 2). Since most of the bottle would be incinerated by 600 °C, the specified heating rate of 15 °C/min to 750 °C was retained. The furnace was held at 750 °C for 8 h to burn off any carbon from the particle coatings and oxidize the kernel material.

Table 2. Heating ramp used to incinerate LDPE in SPEX™ mill bottles and oxidize particle debris

Start Temperature	End Temperature	Ramp Rate	End Temperature Hold Time
25 °C	300 °C	15 °C/min	15 min
300 °C	600 °C	1 °C/min	0 h
600 °C	750 °C	15 °C/min	8 h

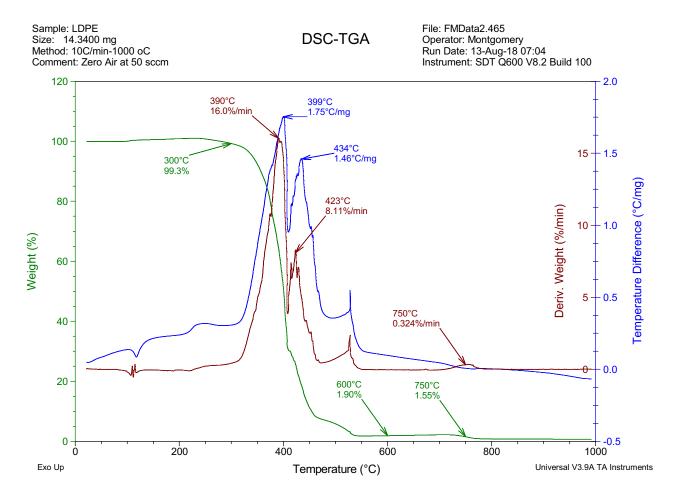


Figure 5. TGA/DTA of the decomposition of LDPE in air.

2.4 LEACHING WITH A SOXHLET EXTRACTOR

To avoid contamination from the manipulator grips, a pickup tool that fits into the slots in the top of the thimble was used to transfer the thimble containing the oxidized sample to the body of the 70 ml Soxhlet apparatus shown in Figure 6. About 100 ml of 67–70% concentrated MilliporeSigma Omnitrace® nitric acid was added to the 250-ml flat-bottom boiling flask used during the incineration of the bottle. The flask was fitted with a 45/50 to 24/40 PTFE bushing and attached to the Soxhlet apparatus. Heat was applied from a 250-ml flask heating mantle, boiling the acid in the flask. The acid vapors were condensed by a chilled-water Allihn condenser above the Soxhlet body filling it with acid and submerging the sample inside the thimble. When the liquid level reached the top of the siphon tube on the side of the Soxhlet body, the acid drained down into the 250 ml flask and the filling process began again.

The siphon cycle took about 30 min and washed much of the crushed fine SiC residue through the #2 frit down into the 250 ml boiling flask. The coarser #2 frit was used because, preliminary testing showed that this fine SiC plugged a #3 frit (15–40-µm porosity) and reduced the amount of acid that could flush through the frit during the siphon cycle. About 50% of the extraction acid flushed through the #2 frit at the end of each cycle. The samples were extracted for 24 h and then the extraction acid was collected in a previously labeled and tared sample bottle.

To verify the completeness of the extraction a second 24 h extraction was performed using an additional 100 ml of nitric acid. At the end of this second extraction there were about 30 ml of acid remaining in the Soxhlet. To collect this residual acid, the thimble was removed, and heat was applied to initiate a final flush of the Soxhlet without any holdup by the frit. The second extraction acid was collected in a separate previously labeled and tared sample bottle. The thimble and flask were rinsed with nitric acid and a small amount of high-purity water (ThermoFisher Scientific NERLTM Type 1). These rinses were added to the second extraction acid sample bottle.

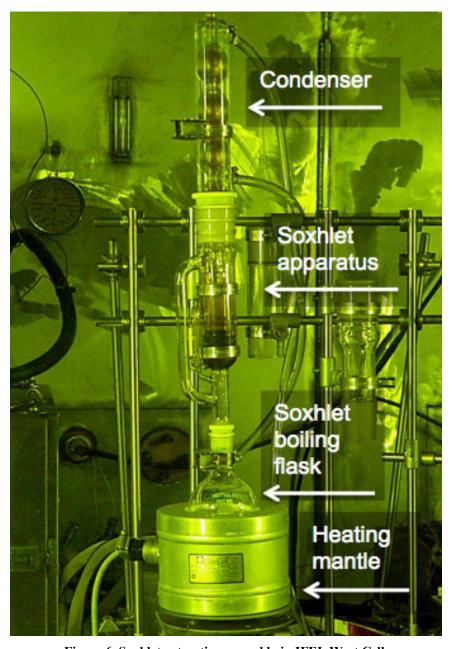


Figure 6. Soxhlet extraction assembly in IFEL West Cell.

2.5 WEIGHING EXTRACTION SAMPLES AND PREPARING ALIQUOTS FOR NACIL

Each extraction acid sample had to be weighed so that analytical chemistry data on the isotopic concentration (measured as a mass fraction) could be converted to the total dissolved mass in each extraction sample. The bottles containing the first and second extraction samples were transferred from the IFEL main hot cell to the radiological hood in the IFEL charging area to be weighed. As with all previous weighing, to assure accurate weights, the balance was verified with check weights before and after the sample weighing. After weighing, the extraction sample bottles were transferred back into the hot cell and aliquots were taken from each sample to provide lower dose subsamples for transfer to NACIL. Each aliquot consisted of 30–50 ml of the extraction acid and was poured into a previously labeled aliquot bottle that had been stored in the hot cell enclosed in a plastic bag to lessen the possibility of radiological contamination. The bottles with the analysis aliquots were removed from the cell, decontaminated with wet wipes, and sent to the NACIL laboratory for gamma spectroscopy and wet chemical analyses as described in Section 3.

3. NACIL EXPERIMENTAL PROCEDURE

Extraction aliquots were analyzed for plutonium via isotope-dilution inductively-coupled-plasma mass spectrometry (ID-ICP-MS) and for uranium primarily by Davies-Gray titration. Neodymium concentration and isotopic composition were determined via an online direct-injection isotope-dilution high-pressure-ion-chromatography inductively-coupled-plasma mass spectrometry (ID-HPIC-ICP-MS) technique. The concentration measurements of these specific elements and their associated isotopic compositions are necessary for employing the calculations needed to determine fuel burnup using the ASTM E321-96(2012), *Standard Test Method for Atom Percent Fission in Uranium and Plutonium Fuel (Neodymium-148 Method)*. The isotopes of uranium, plutonium, and neodymium that were measured in the aliquots are listed in Table 3.

-	·
Element	Analyzed isotopes
Uranium	233, 234, 235, 236, 238
Plutonium	238, 239, 240, 241, 242
Neodymium	142, 143, 144, 145, 146, 148, 150

Table 3 Isotopes analyzed relevant to ASTM E321-96(2012)

All solutions were analyzed for plutonium and uranium using a quadrupole ICP-MS instruments (ThermoFisher Scientific iCAP-RQ). Fuel aliquots and enriched spike solutions were weighed to four decimal places on the same day. Any dilutions performed were also determined by weighing the solutions. Dilutions were made using ThermoFisher Scientific OptimaTM nitric acid and >18.2 M Ω -cm high-purity type I deionized water from a MilliporeSigma Milli-Q® water purification system.

Some ICP-MS analyses were performed of other isotopes for possible future comparative burnup calculations (¹³⁹La, ¹⁴⁰Ce, ¹⁴¹Pr, ¹⁴²Ce, ¹⁵²Sm, and ¹⁵³Eu). These analyses were made using external standardization via linear regression with commercially available standards from High Purity Standards. The samples were prepared by weighted aliquots and analyzed over separate days and multiple dilutions. An internal standard of ¹¹⁵In was employed for matrix correction, though none was noted.

3.1 URANIUM ANALYSIS

Uranium isotopic contributions for the aliquots from the first extraction solutions were determined using ICP-MS and the total uranium content was measured using Davies-Gray titration. The uranium content in the second extraction solutions was analyzed by ID-ICP-MS using an enriched spike solution of ²³³U (New Brunswick Laboratory CRM 111-A) as the isotope dilution internal standard.

Davies-Gray titration was done with slight modifications to ASTM C1201-14, *Standard Test Method for Uranium in Presence of Plutonium by Iron(II) Reduction in Phosphoric Acid Followed by Chromium(VI) Titration.* The standard procedure was developed using aliquots containing 20–50 mg of uranium but samples containing about 2.5 mg of uranium have been successfully titrated [ASTM C1204-14]. Because of restrictions on the radiological dose rates in the ORNL NACIL laboratory, the standard Davies-Gray titration procedure was modified slightly to give accurate uranium concentrations on aliquots containing only 5–10 mg of uranium. This involved adjustments to preserve the accuracy and precision of weighing smaller control samples and titrant quantities. Potassium dichromate titrant and uranium standard controls were gravimetrically diluted by approximately 10× and 20× respectively. Table 4 shows approximate working solution concentrations prepared to maintain accuracy and precision when performing titrations at Low-Low, and Low uranium levels.

Table 4. Davies-Gray working titrant and standard control concentrations

Davies-Gray Solution	Uranium Control Standard	Titrant
Low-Low Level (5 mg U)	0.5259 mg/g solution	0.2125 mg/g solution
Low Level (20 mg U)	10.0976 mg/g solution	1.5171 mg/g solution

The titrant equivalency (f_n) is defined by Equation 1.

 $f_n = (\text{mg U in solution}) / (g \text{ titrant used to reach equivalence point})$ (Equation 1)

Figure 7 shows an example f_n curve for the Low-Low Level titrant concentration in Table 4 and illustrates the sensitivity of f_n on the mass of uranium in the analyzed aliquot. The effect of uranium mass on f_n for analyzed aliquots was taken into consideration by analyzing the sample aliquots and the uranium control standards at similar uranium levels so that the titrant equivalency determined from the control standard would be relevant to the sample aliquot.

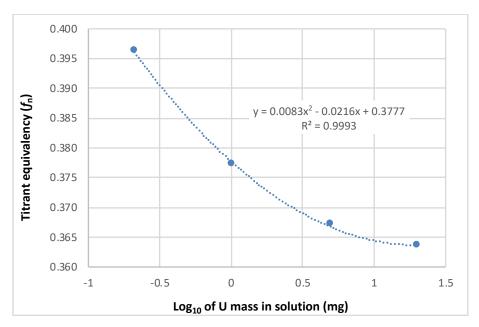


Figure 7. Dependency of titrant equivalency on mass of uranium in Davies-Gray analysis solution.

3.2 PLUTONIUM ANALYSIS

Plutonium was determined in the first extraction solutions using ID-ICP-MS after chemical separation with a Bio-Rad AG®MP-1 Anion Exchange Resin 50–100 mesh (chloride form), which had been converted to the nitrate form. A second aliquot from the first extraction solutions was spiked with enriched ²⁴²Pu (New Brunswick Laboratory CRM 130) as the isotope dilution internal standard. The second extraction solutions were analyzed for plutonium using linear regression calibration ICP-MS and CRM 130 as the calibration standard. The wt% ²⁴⁰Pu was determined for the first extraction solution with the isotopic composition obtained from the resin-separated plutonium aliquot used for ID-ICPMS and applied to the calibrated ²⁴⁰Pu response of the second extraction solution to determine total plutonium. The ²³⁸Pu was measured via alpha pulse height in the chemically-separated aliquot, along with a ²³⁹Pu/²⁴⁰Pu total via alpha spectrometry, and compared to the mass ratio determined in the ICP-MS fraction. The mass ratio was converted to total ²³⁹Pu + ²⁴⁰Pu activity and used in determination of ²³⁸Pu content according to ASTM C1415-18, *Standard Test Method for* ²³⁸Pu *Isotopic Abundance by Alpha Spectrometry*.

3.3 NEODYMIUM ANALYSIS

An online-separation/direct-analysis scheme was used to determine both the concentration and isotopic composition of the neodymium in the first extraction solutions, which were the primary leach of the fuel. The method elementally isolates the neodymium from all natural, non-natural, and polyatomic isobaric interferences yielding a precise isotopic composition. An enriched ¹⁵⁰Nd standard was added (ORNL Isotope Business Office) to determine elemental concentration with high accuracy. The second extraction solutions were analyzed using linear regression ICP-MS and a natural neodymium standard from High Purity Standards. The ¹⁴⁵Nd isotope wt%, determined via HPIC separation of the first extraction solution, was applied to the calibrated response of ¹⁴⁵Nd in the second extraction solution to determine total neodymium in that solution.

The equipment employed for the ID-HPIC-ICPMS was a ThermoFisher Scientific DionexTM ICS-5000⁺ HPIC system coupled to a ThermoFisher Scientific iCAPTM Q quadrupole ICP-MS. The HPIC system is comprised of a DionexTM AS-AP Autosampler, complete with sample dilution and fraction collection capabilities, a gradient mixing pump capable of combining four different eluents in the same analysis, and a thermal compartment containing the injection loop and separation column able to maintain temperatures of 5–85 °C for constant elution times and reproducibility (measurements were performed at 35 °C).

Eluents for HPIC and all other solutions were prepared with trace-metals-basis grade chemicals and ultrapure water (18.2 M Ω -cm) from a MilliporeSigma Milli-Q $\mathbb R$ water purification system. Chemicals for eluents included recrystallized >98% diglycolic acid ($C_4H_6O_5$) (Acros Organics lot A0353334) and 99.999% oxalic acid ($C_2H_2O_4$) (Sigma-Aldrich lot MKCC3466). These were dissolved in ultra-pure water, then buffered with ammonium hydroxide (20–22% as NH $_3$) (ThermoFisher Scientific lot 7115080), to a final pH of 4.6–4.8. The gradient elution profile is described in Table 5 and Figure 8. The resultant chromatograms of the unspiked and spiked aliquots from the first extraction of AGR-2 Compact 2-2-2 particle sample 222-A are provided in Figure 9 as an example of the elemental separation.

Table 5: Elution profile for the elemental separation of neodymium from all isobaric interferences

Interval Type	Time (s)	Deionized H ₂ O (%)	6 mM Diglycolic Acid (%)	150 mM Oxalic Acid (%)
Start	0	100	0	0
Ramp	300	40	0	60
Hold	540	40	0	60
Ramp	546	20	0	80
Ramp	1080	51	23	26
Ramp	1380	0	100	0

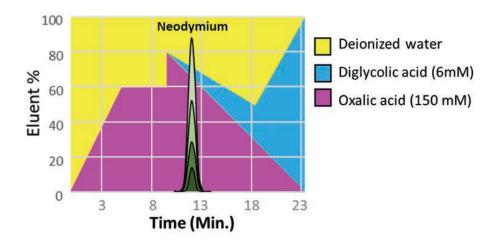


Figure 8. Graphical representation of the relative abundance of eluents as a function of time for the elution profile (Table 5) used in the HPIC elemental isolation of neodymium showing the neodymium elution point.

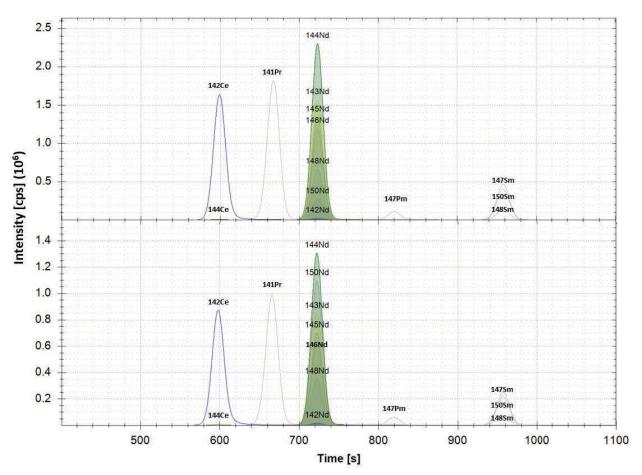


Figure 9. Chromatograms of the unspiked aliquot (above) and ¹⁵⁰Nd-spiked aliquot (below) from the first extraction of AGR-2 Compact 2-2-2 particle sample 222-A illustrating the separation between the isotopes of neodymium and the isobaric interferences ¹⁴²Ce, ¹⁴⁴Ce, ¹⁴¹Pr, ¹⁴⁷Pm, ¹⁴⁷Sm, ¹⁴⁸Sm, and ¹⁵⁰Sm.

4. RESULTS AND CALCULATION OF BURNUP

The method in ASTM E321-96(2012) covers measurement of the stable fission product ¹⁴⁸Nd to calculate burnup in uranium fuel with an allowable plutonium content up to 50%. The total heavy element atom percent fission (F_T), or %FIMA, is given by Equation 2, where F' is the number of atoms in the fuel that underwent fission and U' and Pu' are the atoms of uranium and plutonium remaining after irradiation. The sum of U', Pu', and F' provides a reasonably accurate determination of the initial heavy metal content of the fuel with negligible error introduced by ignoring the other minor constituents (\sim 0.14% error for Compact 2-2-2 and \sim 0.07% error for Compact 6-4-2, based on calculated actinide inventory [Sterbentz 2014]).

$$F_T = [F'/(U' + Pu' + F')] \times 100$$
 (Equation 2)

The number of fissioned atoms F' can be calculated with Equation 3, where $FY_E(^{148}Nd)$ is the effective fractional fission yield of ^{148}Nd . The ^{148}Nd atoms from fission is determined by correcting the measured atoms of ^{148}Nd for natural contamination and production of ^{148}Nd by the $^{147}Nd(n,\gamma)^{148}Nd$ neutron capture reaction. The natural contamination correction is determined by measuring the content of the shielded isotope ^{142}Nd . The effective fractional fission yield of ^{148}Nd is the weighted sum of the fractional fission yield of ^{148}Nd from each heavy metal isotope, with weighting based on each isotope's contribution to the total number of fissions.

$$F' = (^{148}Nd \text{ atoms from fission}) / FY_E(^{148}Nd)$$
 (Equation 3)

The dominant contribution to fission production of 148 Nd in the AGR-2 fuel comes from the thermal neutron fissions 235 U_{th}, 239 Pu_{th}, and 241 Pu_{th} and the fast neutron fission 238 U_{fast}. The individual fractional fission yields of 148 Nd from these four fission events, the fractional contribution of each to the total number of fissions, and the calculated effective 148 Nd fractional fission yields for AGR-2 Compacts 2-2-2 and 6-4-2 are given in Table 6. Ignoring the other fissioning isotopes introduces a negligible error of less than 0.05%. The fractional contribution of each fission event to the total number of fissions was based on the AGR-2 daily depletion simulation [Sterbentz 2014] but any error in the values used is minimized by the fact that the thermal neutron fissions 235 U_{th} and 239 Pu_{th} have similar cumulative fission yields for 148 Nd.

Fission	TW 44831 1\ a	AGR-2 Compact 2-2-2		AGR-2 Compact 6-4-2	
event $FY(^{148}Nd)^a$		% Total ^b	$FY_E(^{148}Nd)$ contribution	% Total b	$FY_E(^{148}Nd)$ contribution
$^{235}U_{th}$	$1.6735E-02 \pm 5.9E-05$	79.68%	$1.333E-02 \pm 4.7E-05$	85.92%	$1.438E-02 \pm 5.0E-05$
$^{238}U_{\text{fast}}$	$2.1125E-02 \pm 1.5E-04$	0.40%	$8.545E-05 \pm 6.0E-07$	0.36%	$7.674E-05 \pm 5.4E-07$
$^{239}Pu_{th} \\$	$1.6421E-02 \pm 8.2E-05$	17.22%	$2.827E-03 \pm 1.4E-05$	12.69%	$2.084\text{E-}03 \pm 1.0\text{E-}05$
$^{241}Pu_{th} \\$	$1.9321E-02 \pm 1.4E-04$	2.66%	$5.134E-04 \pm 3.6E-06$	1.00%	$1.924E-04 \pm 1.3E-06$
Other	<2E-02	0.04%	<8E-06	0.03%	<6E-06
		Compact 2-2-2 <i>FY_E</i> (¹⁴⁸ Nd)		Compact 6-4-2 <i>FY_E</i> (¹⁴⁸ <i>Nd</i>)	
$1.676E-02 \pm 5$		$.676E-02 \pm 5E-05$	1.	$673E-02 \pm 5E-05$	

Table 6. Calculation of effective fractional fission yield for 148Nd

A table of factors to correct for the 147 Nd(n, γ) 148 Nd neutron capture reaction based on the neutron flux and fluence is provided in ASTM E321-96(2012). However, the table does not cover the irradiation conditions that were obtained in the AGR-2 irradiation. Suyama and Mochizuki have calculated the effect of the

^a Cumulative fission yields from ENDF/B-VII.1 [Chadwick et al. 2011] were downloaded from www.nndc.bnl.gov.

^b The percent each isotope contributed to the total fission was based on AGR-2 physics calculations [Sterbentz 2014].

 147 Nd(n, γ) 148 Nd neutron capture reaction on 148 Nd production as a function of the neutron flux and fluence over a range relevant to the AGR-2 samples [Suyama and Mochizuki 2005]. Table 7 shows the estimated total neutron fluence and flux for each sample, where the total neutron fluence was estimated to be five times the fast fluence given in Table 1 and the flux was estimated to be constant over the AGR-2 irradiation period. The percentage of 148 Nd produced by the 147 Nd(n, γ) 148 Nd neutron capture reaction during irradiation was taken from Figure 3 of [Suyama and Mochizuki 2005] using these estimated total neutron fluence and flux values and was used to adjust the contamination-corrected amount of 148 Nd measured in each sample to account for the 148 Nd from neutron capture. The cross sections for 146 Nd(n, γ) 147 Nd and 148 Nd(n, γ) 149 Nd are more than two orders of magnitude lower than that for 147 Nd(n, γ) 148 Nd [Chadwick et al. 2011], so corrections for these reactions were not necessary.

Table 7. Estimated factor to correct ¹⁴⁸Nd inventory for ¹⁴⁷Nd(n,γ)¹⁴⁸Nd neutron capture reaction

	AGR-2 Compact 2-2-2	AGR-2 Compact 6-4-2
Fluence (n/m²) a	1.7E26	1.1E26
Flux (n/m ² s) ^b	3.5E18	2.3E18
$^{148}Nd \ from \ ^{147}Nd(n,\gamma)^{148}Nd$	2.9%	1.9%

^a Total neutron fluence estimated as 5×fast fluence from Table 1.

Appendix A shows the measurement results for the total inventory extracted from each riffled particle sample of the uranium, plutonium, and neodymium isotopes used in the burnup calculation following the 148 Nd method in ASTM E321-96(2012). The calculated burnups are shown in the last row of Table 8. Also included in the table are values that show the impact of not performing the necessary corrections for the conflicting sources of 148 Nd. The first row shows the burnup values based on using the as-measured 148 Nd with no correction for natural contamination or production of 148 Nd by the 147 Nd(n, γ) 148 Nd neutron capture reaction when calculating F' in Equation 3. The second row only includes the correction for natural contamination. A small amount of natural 142 Nd was detected in the extraction samples. The 142 Nd isotope is not formed significantly through fission because it is shielded by stable 142 Ce. This makes it a convenient marker for natural contamination. Naturally-occurring neodymium is 27.152% 142 Nd and 5.756% 148 Nd [Berglund and Wieser 2011]. Based on the concentration of 142 Nd measured in each sample, the amount of 148 Nd from natural contamination was calculated by Equation 4 and subtracted from the measured amount of 148 Nd.

$$^{148}Nd_{contamination} = (^{142}Nd/0.27152) \times 0.05756$$
 (Equation 4)

Table 8. Burnup in %FIMA based on fission production of ¹⁴⁸Nd for AGR-2 Compacts 2-2-2 and 6-4-2

Compostions Applied		Particl	e sample	
Corrections Applied	222-A	222-В	642A	642B
no corrections	13.12 ± 0.22	13.19 ± 0.26	10.28 ± 0.20	9.81 ± 0.19
just natural Nd contamination	12.97 ± 0.22	13.04 ± 0.26	10.20 ± 0.20	9.74 ± 0.19
all corrections	12.64 ± 0.25	12.71 ± 0.29	10.03 ± 0.22	9.57 ± 0.21

^b Total neutron flux estimated by multiplying estimated total neutron fluence by 559.2 effective full power days [Collin 2014].

^c Correction factor taken from Figure 3 of [Suyama and Mochizuki 2005].

5. RECOMMENDED NEXT STEPS

Other stable fission product isotopes can also be used to compute the number of fissions that occur during irradiation. Several methods for calculation of nuclear fuel burnup in TRISO particles were explored during AGR-1 PIE [Harp et al. 2014]. These included non-destructive gamma spectroscopy methods and destructive chemical analysis followed by mass spectroscopy. Six isotopes were identified by Harp et al. as reliable fission indicators for the AGR fuel: ¹³⁹La, ¹⁴⁰Ce, ¹⁴²Ce, ¹⁴¹Pr, and the sum of ¹⁴⁵Nd and ¹⁴⁶Nd. Additional calculations should be performed to calculate burnup using these and other isotopes that were measured during the AGR-2 Compact 2-2-2 and 6-4-2 sample analyses.

As mentioned in Section 3, several isotopes (¹³⁹La, ¹⁴⁰Ce, ¹⁴¹Pr, ¹⁴²Ce, ¹⁵²Sm, and ¹⁵³Eu) were measured using a typical external standardization ICP-MS technique in addition to the high-accuracy measurements of the neodymium isotopes by isotope dilution and ion-exchange chromatography. The data available for isotopes other than ¹⁴⁸Nd offer additional opportunities for comparative calculation of the burnup in these samples. As was done for ¹⁴⁸Nd, these calculations should include, where possible and necessary, corrections for natural contamination and production/destruction of the fission indicating isotope due to neutron capture. Neutron capture correction factors for each isotope could be based on estimations from known cross sections for the relevant reactions, as was done for ¹⁴⁸Nd in ASTM E321-96(2012). However, a more direct estimation of the correction factor might be obtained by extracting information on the fraction of each isotope that was formed and lost during the AGR-2 irradiation test from the daily depletion simulation [Sterbentz 2014]. The availability of the necessary simulation data has been confirmed and the extraction of the relevant information will only require modification of the data post-processors.

Comparisons of the burnup estimates obtained from the available isotope data can be compared with consideration of the preferred properties of a burnup indicator as discussed in ASTM E321-96(2012) and [Harp et al. 2014].

- 1) Low volatility or diffusive release of the isotope and its precursors is preferred. Previously obtained safety testing and LBL data is available for AGR-2 Compacts 2-2-2 and 6-4-2 that provide information on fractional loss of most of the isotopes of interest and will help interpret some of the differences that may be observed between the various burnup calculations. Diffusive release of ¹⁵³Eu is a particular issue for Compact 2-2-2, which was irradiated at a temperature that increased diffusive release during the irradiation test to above 10%.
- 2) All isotopes currently of interest are stable isotopes and this simplifies the analysis in that decay correction is not required.
- 3) Low cross sections for neutron capture that result in production or destruction of the fission indicator is preferable. Where cross sections are higher, availability of an accurate correction factor is important. A comparative study will highlight the impact of high cross sections for some isotopes, such as $^{151}\text{Sm}(n,\gamma)^{152}\text{Sm}$ and $^{152}\text{Eu}(n,\gamma)^{153}\text{Eu}$, which have cross sections around 10 kb.
- 4) ASTM E321-96(2012) identifies that ¹⁴⁸Nd has good characteristics for mass spectrometry. This can be considered for the other isotopes of interest.
- 5) Fission yields from ²³⁵U and ²³⁹Pu should be similar and high yields can reduce measurement uncertainty.
- 6) Low contamination or a convenient shielded isotope, such as ¹⁴²Nd, for contamination correction is important for maximum accuracy.
- 7) It is important that the isotope of interest have a high solubility in the leachate. Concentrated nitric acid was used for the extractions performed on the particle samples from Compact 2-2-2 and 6-4-2. Addition of other acids, such as HF and HCl, or variation in the sample preparation methods prior to leaching can increase the solubility of some elements. Harp et al. studied the addition of HF and variation of the burn temperature.

6. CONCLUSIONS

A procedure was developed and approved to pulverize and leach isotopes for burnup calculations from TRISO particle fuel samples using the ORNL IFEL hot cell facilities [Montgomery and Hunn 2018]. This procedure was applied to two ~200-particle samples taken from the burn-leach archives of 1600°C safety-tested AGR-2 Compacts 2-2-2 and 6-4-2. The samples were analyzed for uranium, plutonium, and neodymium using Davies-Gray titration and ICP-MS methods designed to produce high-accuracy data through the use of isotope dilution for internal standardization. Additional accuracy was obtained in the neodymium analysis using a ThermoFisher Scientific DionexTM ICS-5000⁺direct-injection HPIC system coupled to the ICP-MS to isolate the neodymium isotopes from isobaric interferences from other isotopes via ion chromatography. Burnup was calculated from the data using the in ASTM E321-96(2012) ¹⁴⁸Nd method.

According to ASTM E321-96(2012), ¹⁴⁸Nd is considered an ideal candidate for burnup analysis because of its low volatility, good characteristics for mass spectrometry, similar fission yield from ²³⁵U and ²³⁹Pu, and availability of the ¹⁴²Nd shielded isotope for natural-neodymium contamination correction. The preferred property of low volatility was further bolstered by previously-performed LBL and safety testing, which showed inconsequential loss of neodymium (as well as uranium and plutonium) from the fuel particles prior to its extraction for the burnup analysis (releases were <0.1% for Compact 2-2-2 and <0.01% for Compact 6-4-2).

Also critical for the accurate determination of burnup via 148 Nd analysis is accurately accounting for the 147 Nd(n, γ) 148 Nd neutron capture reaction. If not accurately determined, this correction could introduce a systematic error of several percent. A correction was estimated based on a paper by Suyama and Mochizuki and the average neutron flux and fluence for Compacts 2-2-2 and 6-4-2. A more rigorous correction can be determined from the daily depletion simulation [Sterbentz 2014] and that effort is in progress. Obtaining the correction for neutron capture in this manner will also account for the fact that the 11-day half-life 147 Nd decayed significantly during the reactor shutdowns that occurred throughout the AGR-2 irradiation test and the impact of reactor shutdowns were not accounted for in the continuous-irradiation calculation by Suyama and Mochizuki.

Table 9 shows the calculated burnup in %FIMA for the analyzed samples and compares the average to the burnup estimated with the JMOCUP Monte Carlo depletion methodology [Sterbentz 2014]. The calculated burnup via the ¹⁴⁸Nd method was higher than the values obtained by the daily as-run physics depletion model [Sterbentz 2014]. Agreement between Sample 222-A and Sample 222-B was very good and well within the estimated uncertainty. However, this was not the case for the two Compact 6-4-2 samples, which deviated by almost 5%. The dominant source of this deviation may have been in the measurement of the remaining uranium, which was the largest value in Equation 2 and differed between Sample 642-A and 642-B by 8% (Appendix A). Analysis of three samples from each compact was originally planned but was reduced to two to reduce the time and cost required for the analysis, based on the preliminary results from the first two Compact 2-2-2 samples exhibiting a deviation below the measurement uncertainty. The analysis of Compact 6-4-2 would benefit from inclusion of analysis of the third 200-particle sample taken from that compact, as this might elucidate whether one of the other results was impacted by an abnormal error.

Table 9. Results of burnup analysis via the ASTM E321-96(2012) ¹⁴⁸Nd method (%FIMA)

Compact	Sample A	Sample B	Average	[Sterbentz 2014]
AGR-2 2-2-2	12.64 ± 0.25	12.71 ± 0.29	12.68 ± 0.19	12.55
AGR-2 6-4-2	10.03 ± 0.22	9.57 ± 0.21	9.80 ± 0.15	9.26

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APPENDIX A. EXPERIMENTALLY MEASURED ELEMENTAL MASS AND ISOTOPE FRACTIONS

Isotope	Sample 222-A	Sample 222-B	Sample 642-A	Sample 642-B
total U (mg)	69.275 ± 0.105	67.679 ± 0.088	64.083 ± 0.115	69.570 ± 0.124
²³³ U (at%)	0.0000 ± 0.0000	0.0000 ± 0.0000	0.0000 ± 0.0000	0.0000 ± 0.0000
²³⁴ U (at%)	0.1060 ± 0.0021	0.1067 ± 0.0021	0.1201 ± 0.0024	0.1213 ± 0.0024
²³⁵ U (at%)	2.7732 ± 0.0555	2.7954 ± 0.0559	5.3096 ± 0.0531	5.3814 ± 0.0538
²³⁶ U (at%)	2.1400 ± 0.0428	2.1734 ± 0.0435	1.6901 ± 0.0338	1.6977 ± 0.0339
²³⁸ U (at%)	94.9808 ± 0.9498	94.9245 ± 0.9492	92.8802 ± 0.9288	92.7996 ± 0.9280
total Pu (mg)	1.0188 ± 0.0201	0.9694 ± 0.0191	0.8976 ± 0.0020	1.0229 ± 0.0029
²³⁸ Pu (at%)	1.8382 ± 0.0367	1.8027 ± 0.0361	0.8980 ± 0.045	0.7182 ± 0.036
²³⁹ Pu (at%)	51.0348 ± 0.5104	50.9938 ± 0.5099	62.9658 ± 0.630	63.2226 ± 0.632
²⁴⁰ Pu (at%)	27.9560 ± 0.2796	27.9881 ± 0.2799	25.8848 ± 0.259	25.9246 ± 0.259
²⁴¹ Pu (at%)	11.4198 ± 0.1142	11.4864 ± 0.1149	7.7148 ± 0.077	7.6321 ± 0.153
²⁴² Pu (at%)	7.7512 ± 0.0775	7.7291 ± 0.0773	2.5366 ± 0.051	2.5026 ± 0.050
²⁴⁴ Pu (at%)	0.0000 ± 0.0000	0.0000 ± 0.0000	0.0000 ± 0.000	0.0000 ± 0.000
total Nd (mg)	1.2605 ± 0.0070	1.2298 ± 0.0144	0.8952 ± 0.0093	0.9230 ± 0.0102
¹⁴² Nd (at%)	0.5411 ± 0.0054	0.5429 ± 0.0054	0.3175 ± 0.0064	0.3132 ± 0.0063
¹⁴³ Nd (at%)	17.7622 ± 0.1776	17.7307 ± 0.1773	21.8339 ± 0.2183	22.1606 ± 0.2216
¹⁴⁴ Nd (at%)	35.8937 ± 0.3589	35.9966 ± 0.3600	32.1685 ± 0.3217	31.9225 ± 0.3192
¹⁴⁵ Nd (at%)	17.0592 ± 0.1706	16.9449 ± 0.1694	18.0614 ± 0.1806	18.0611 ± 0.1806
¹⁴⁶ Nd (at%)	16.6424 ± 0.1664	16.5791 ± 0.1658	15.8016 ± 0.1580	15.7235 ± 0.1572
¹⁴⁸ Nd (at%)	8.5791 ± 0.0858	8.6391 ± 0.0864	8.4602 ± 0.0846	8.4603 ± 0.0846
¹⁵⁰ Nd (at%)	3.5223 ± 0.0358	3.5668 ± 0.0357	3.3570 ± 0.0336	3.3587 ± 0.0336